

**Attachment B**  
***Experimental Design Protocol***

## Overview

This document provides an overview of a lab experiment that examines the cost-effectiveness of alternative auction design mechanisms for an auction environment resembling USDA's Conservation Reserve Program's (CRP's) General Signup. The CRP General Signup is a multi-unit, pay-as-bid, reverse auction. A consequence of the multi-unit, pay-as-bid approach is that the CRP runs a risk of paying substantial information rents. Currently the CRP uses a bid-cap approach based on estimates of reserve values to limit information rents. The goal of this research is to investigate the performance of alternative auction mechanisms designed to limit information rents. Conceptually, most of these mechanisms operate by accepting some higher cost bids to maintain competitive pressure on the lower cost bidders who have the most potential to extract information rents.

## Key Design Terminology

**Experiment** – The *experiment* is composed of multiple 90-minute sessions. The number of sessions in an experiment is determined by the budget for the project and the statistical power required to test the primary research hypotheses.

**Session** – A *session* involves one group of participants, starts when we open the doors of the lab and ends 90 minutes later.

**Treatment** – A *treatment*, for the purposes of this experiment, is a particular auction structure (design). During each session the participants will participate in at least three different treatments, or types of auctions. Each treatment will consist of several rounds of that type of auction. For example, if there are three treatments and each treatment has 15 rounds, then a given session would consist of 45 total rounds. Each round takes on average 100 seconds, which leaves 15 minutes to provide participants with information about how the different auctions and the payoff structure operate.

**Round** – There will be multiple auctions, or *rounds* in each session. More rounds per treatment will allow for individuals to learn about both the incentive structure in each treatment as well as to update their beliefs about the distribution of valuation among the other participants in each auction. However, more rounds per treatment also limit the number of treatments that can be included per session.

**Information rents:** Participants within the experiment may learn how to use the information they acquire strategically to receive a rental payment in excess of their costs – in excess over a normal market rent. This information rent will increase the cost to the buyer in the auction.

## Experiment structure

- Z-tree interface with internet administration

- 12 experimental sessions, 16 participants per session
- 3 treatments per session up to 20 rounds (based on previous similar experiments, we predict an average of 15 rounds of each treatment, but subjects between sessions often proceed at different speeds, making 20 rounds possible in some circumstances; in all cases we will maintain a 90 minute maximum experiment time.)
- Random order of treatment within session
- Total of 5 treatments to be tested
  1. Baseline (tight bid cap)
  2. Loose cap
  3. Reference price
  4. Endogenous reference price
  5. Grouping

Session	Treatment*	Average # of rounds per treatment	Max # of rounds per treatment	Time (in minutes)	# of participants
1	1,2,3	12	15	90	16
2	1,2,4	12	15	90	16
3	1,2,5	12	15	90	16
4	1,3,4	12	15	90	16
5	1,3,5	12	15	90	16
6	1,4,5	12	15	90	16
7	1,2,3	12	15	90	16
8	1,2,4	12	15	90	16
9	1,2,5	12	15	90	16
10	1,3,4	12	15	90	16
11	1,3,5	12	15	90	16
12	1,4,5	12	15	90	16

\* Random order of treatment within session.

### Payment

We will normalize payment so that the average payment is \$25 per 1.5 hour session.

In the pretest for ICR 201411-0536-001, a similar experiment to the one proposed here, the average earnings were 45.81 Experimental Currency Units (ECU), with a minimum payment of 9 and a maximum payment of 106. In order to ensure that the average payment is \$25, this implies a conversion factor of approximately 0.5. That is, one ECU will be worth \$0.50. The high payment in this case would have been \$53 and the low payment \$4.50.

The payments need to be set such that students are compensated for their participation of 1.5 hours. Please see Mini Supporting Statement Part A (section A.9) for a detailed discussion of the payment plan and its justification.

### Auction clearing

The auction will clear based on a fixed unit demand (as opposed to a budget-constrained auction). Assuming 16 participants (sellers) per experiment and a single unit available for each participant to sell, the buyer will accept 8 units. If all participants choose to make a bid, then this will result in a 50 percent bid-acceptance rate.

### Key Auction Terminology

**Unit:** A unit is the item that participants are selling at auction. At the beginning of each round, each participant has one unit to sell.

**Valuation:** The valuation of each unit ( $v_i$ ) is private information about the cost (i.e.: “reserve value” or “opportunity cost”) of each unit. Each participant knows their own valuation, which is given to them at the beginning of a round. Participants do not know each other’s valuations. The buyer does not know any of the participants’ valuations.

**Reference price:** The buyer’s beliefs about the cost of each unit ( $\hat{v}_i$ ) is semi-private information about the buyer’s beliefs. In some treatments, participants learn the buyer’s estimate of their own unit’s value. Participants are *never* told what the buyer believes about the values of other participants’ units. The reason that the buyer’s beliefs are disclosed is that these beliefs are explicit determinants of key parameters in the auction design. For example, in the simplest auction design, the buyer’s estimate (plus a markup) serves as a cap to each individual’s bid.

### Determination of value

The first steps in running each round involve determining each participant’s valuation for the unit that they can offer in that round. The parameterization of the valuation process is an important part of the design of this experiment.

Each unit’s value is determined by the following process:  $v_i$  is drawn from a uniform distribution  $U[10, 110]$ .

The buyer can estimate the valuation  $v_i$  of each of the participants in the auction, and will try to use this information to reduce the total cost of procuring units in the auction. The buyer does not observe any valuation with perfect precision, however. What the buyer actually observes is noisy signal of actual opportunity costs:  $\hat{v}_i = v_i + e_i$ , where  $e_i$  is an error term and  $e_i \in [-5, 5]$ .

### Treatments

1. Baseline (tight bid cap)

$$\text{Bid cap} = \hat{v}_i$$

2. Loose cap

Identical to the baseline treatment, but the maximum bid is equal to

$$\text{Bid cap} = \hat{v}_i + 5$$

3. Reference price ranking

The buyer will use the estimated of value as a *reference price*. In particular, the reference price for each unit is equal to  $\hat{v}_i$ . The score of each bidder is equal to the bid divided by the reference price plus the reference price divided by 150. The buyer will accept the 8 bids with the lowest scores to purchase, and will reject the remaining bids.

4. Endogenous reference price

The reference price for each unit is equal to the average **bid** of neighbor bidders. The score of each bid is equal to the bid divided by the reference price plus the reference price divided by 150. The neighbors of the  $i^{\text{th}}$  bidder is defined as the four nearest-neighbors in terms of the value estimate ( $\hat{v}_i$ ). The buyer will accept the 8 bids with the lowest scores to purchase, and will reject the remaining bids.

5. Grouping

There are a maximum number of bids from each group (A and B) that will be accepted by the buyer. These are parameters controlled by the experimenter. There are 8 bidders in group A and 8 bidders in group B. The 8 bidders with the lowest values of  $\hat{v}_i$  are in group A; the remainder are in group B. The buyer will accept the 8 lowest bids to purchase, unless doing so causes the buyer to accept more than the maximum number of bids from a given group. If the buyer is prevented from purchasing a unit because of the group limit, the buyer will select for purchase the eligible unit (from the other group) with the next-lowest bid.

## Outcomes of interest and power analysis

### Outcomes

(1) Total procurement cost is the primary outcome of interest. Our power analysis is based on this primary outcome (see table and discussion below).

(2) A parameterized bidding function is a secondary outcome of interest. We will use a polynomial function of the value draws to estimate a bidding function  $\text{bid} = b(\text{value})$ .

We will control for fixed factors with session and individual fixed-effects.

## Power analysis

Each experiment will yield a minimum of 12 rounds of data per treatment (three treatments—36 rounds of data). Because the 12 rounds are not independent (the same subjects participate in each of the rounds), we cluster at the session level. That is, the 36 observations generated in each session are not treated as independent. We are interested in the total procurement cost for each auction treatment; we obtain one (non-independent) observation of a given auction outcome each round. The requested number of burden hours allow us to conduct a total of 12 sessions. This means that we are conducting a test of means (mean procurement cost) clustered at the session level (12 clusters).

We have 12 sessions, each session yielding 36 observations. This gives us a total of  $12 * 36 = 432$  observations, or an average of 86 (rounded down) observations per auction treatment.

Based on an estimated average of 241.1 ECUs (Experimental Currency Units) and a standard deviation of 65 for the baseline treatment, the estimated minimum detectable effect (MDE) is 40.20.

The simulations used to determine the average procurement cost of 241.1 and the standard deviation of 65 are copied below in the Appendix.

## Appendix

Simulations to determine expected cost of procurement for the baseline auction were run in the computer programming language R. R is freely available at [www.r-project.org/](http://www.r-project.org/).

```
# What is the procurement cost of a baseline auction? These costs will be the basis of
# comparison to the three treatments
# Calculate based on simulations, with bidding behavior given by game theoretic
# analysis.
# The bidding behavior is given by:
#  $b*_i = cap_i$  if  $v_i < cap_i$  (the bidder will bid the cap if their underlying value is less
# than the cap, unless...
#  $b*_i = 0.3974 + 0.4210 * v_i$  if  $v_i < 0.3974 + 0.4210 * v_i < cap_i$  (the bidder trades off
# the probability of being accepted with receiving a higher payment if their optimal bid is
# less than the cap)
#  $b*_i = v_i$  if  $0.3974 + 0.4210 * v_i < v_i < cap_i$  (bidder will bid exact costs)

# Monte Carlo size
mc <- 10000
```

```
# Create a container variable for the cost of each iteration
cost <- rep(0,mc)

# Set seed
set.seed(12)

# Execute simulation
for (i in 1:mc) {
  # Draw a random sample from [0,1]
  v <- runif(16, min = 0, max = 1)

  # Draw a buyer's estimate of value (equal to the price cap)
  vHat <- v + runif(16, min = 0, max = 1)/20

  # Bidding function
  bTilda <- 0.3974+0.4210*v
  b <- rep(0,16)
  for (j in 1:16) {
    if (v[j] < vHat[j]) {
      b[j] <- vHat[j]
    }
    if ((v[j] < bTilda[j]) & (bTilda[j] < vHat[j])) {
      b[j] <- bTilda[j]
    }
    if ((bTilda[j] < v[j]) & (v[j] < vHat[j])) {
      b[j] <- v[j]
    }
  }
}

# Sort bids from lowest to highest
sb <- b[order(b)]

# Select the 8 lowest and sum the cost of enrolling them
cost[i] <- sum(sb[1:8])
}

# Multiply cost by 100 and add 10 to project onto proper scale
cost <- cost*100 + 10

# The average cost of an auction is:
summary(cost) # 241.10

# The sd of cost is:
```

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sd(cost) # 64.96152